

Integrated Scientific Modeling and Lab Automation

A decorative background consisting of a series of overlapping, semi-transparent, colorful shapes that resemble stylized waves or peaks. The colors include shades of purple, blue, green, yellow, orange, red, and brown, creating a vibrant and layered effect.

Luca Cardelli, University of Oxford
2022-09-27 Applied Systems Biology Course

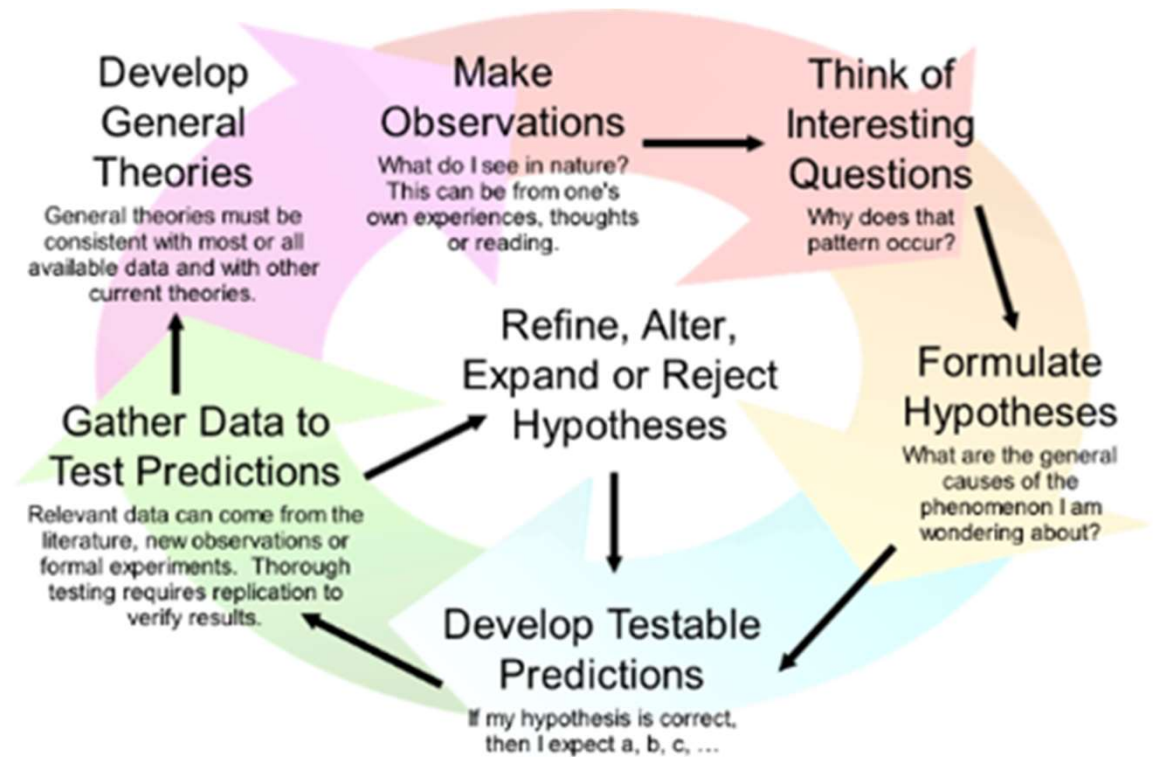
Outline

- The Scientific Method
 - Its eventual automation
- Lab Protocols (that know nothing about models)
 - Digital Microfluidics
- Models (that know nothing about protocols)
 - Chemical Reaction Networks
- Integration
 - Closed-loop modeling and protocol execution

The Scientific Method

Hasan Ibn al-Haytham (1027) Book of Optics

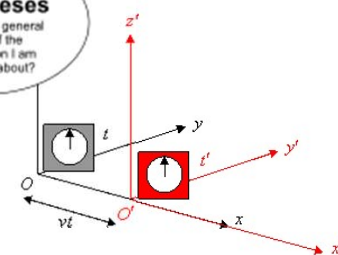
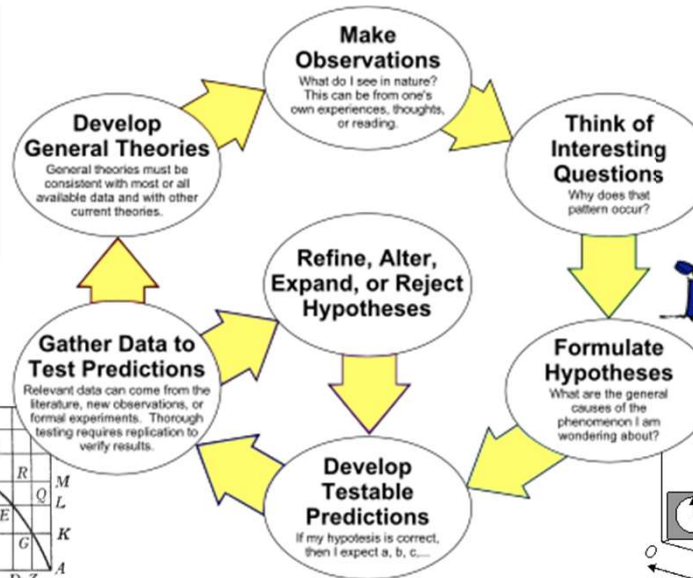
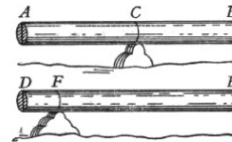
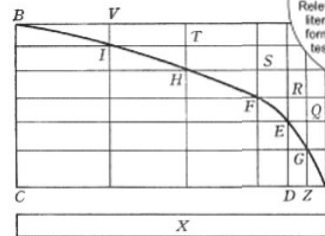
Galileo Galilei (1638) Two New Sciences



Discovery through Observation

The Scientific Method ~ 1638

1 Person



Garland, Jr., Theodore. "The Scientific Method as an Ongoing Process". U C Riverside.

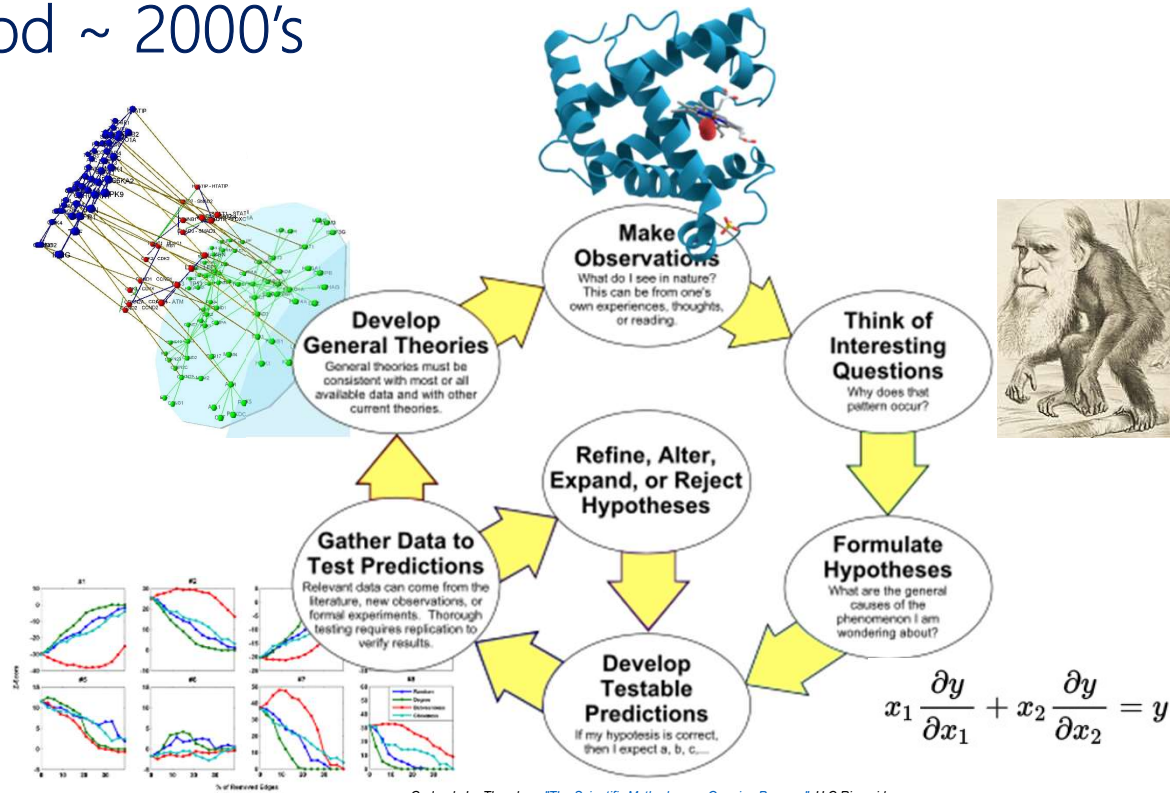
Discovery through Collaboration

The Scientific Method ~ 2000's

1 Lab



1 protein = 30 people / 30 years
 Humans have >250,000 proteins ☹️



$$x_1 \frac{\partial y}{\partial x_1} + x_2 \frac{\partial y}{\partial x_2} = y$$

Garland, Jr., Theodore. "The Scientific Method as an Ongoing Process". U C Riverside.

Discovery through Automation

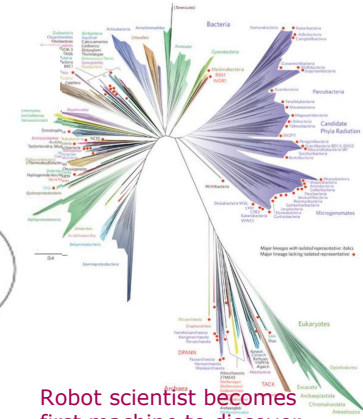
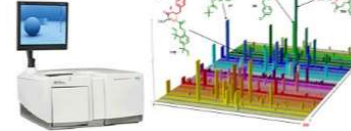
The Scientific Method ~ 2020's

1 Program

```
while (true) {  
  predict();  
  falsify();  
}
```



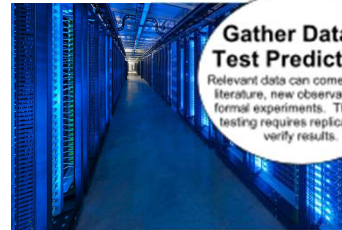
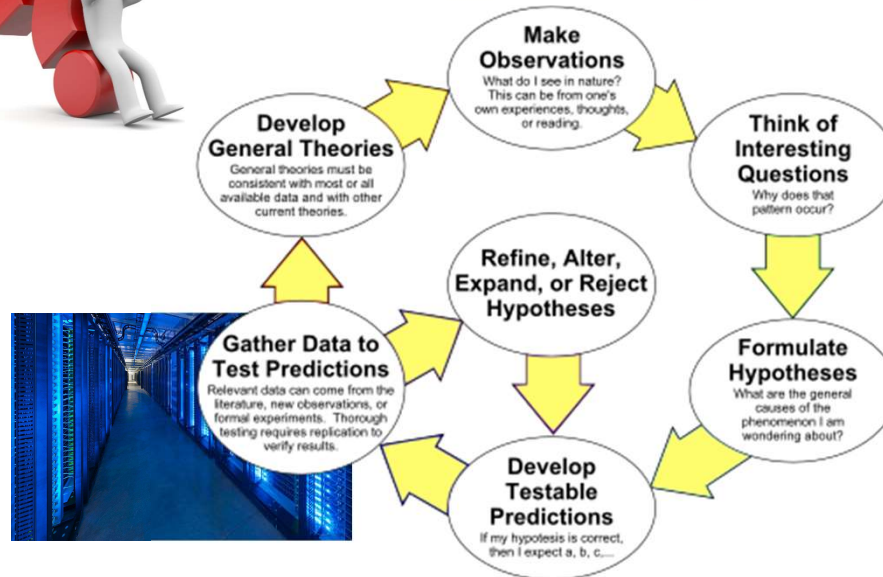
High Throughput sequencing



Robot scientist becomes first machine to discover new scientific knowledge



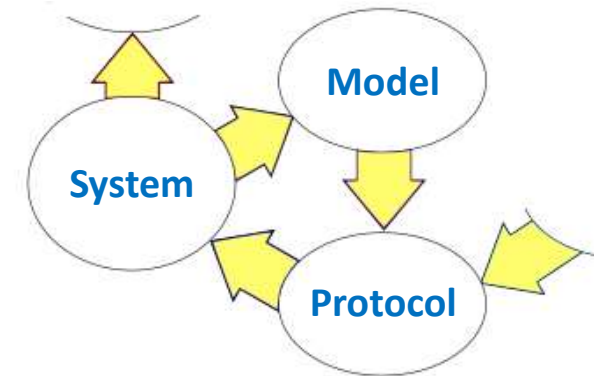
Ross King



Garland, Jr., Theodore. "The Scientific Method as an Ongoing Process". U C Riverside.

The Inner Loop

- A *model* is refined by testing a *protocol* against a *systems*
- A *protocol* is refined by testing a *model* against a *systems*
- Today: **publication does not accurately reflect execution**
 - Model: poorly-maintained matlab script
 - Protocol: poorly-described manual steps in the lab
 - System: poorly-characterized and hardly "resettable"
- ⇒ Crisis in biology: experiments are done once and are hard to reproduce
<http://www.nature.com/news/reproducibility-1.17552>



The Inner Loop

- Tomorrow, **automation**

Nodes

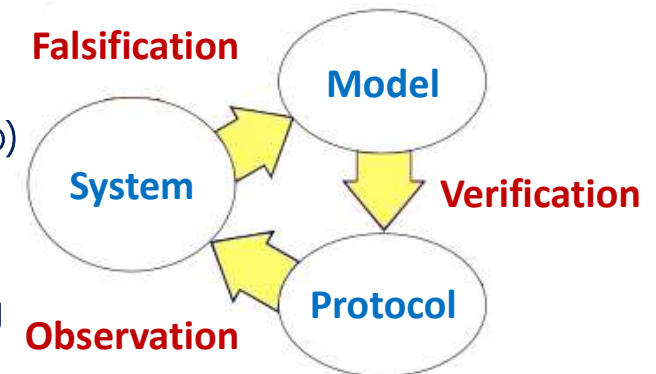
- Model: unambiguous (mathematical) description (CompBio)
- Protocol: standardized (engineered) parts and procedures (SynthBio)
- System: characterized (biological) organism and foundries (SysBio)

Arcs

- Verification: simulation / analysis / model checking / theorem proving
- Observation: lab automation
- Falsification: statistical inference / model reduction

Lifecycle

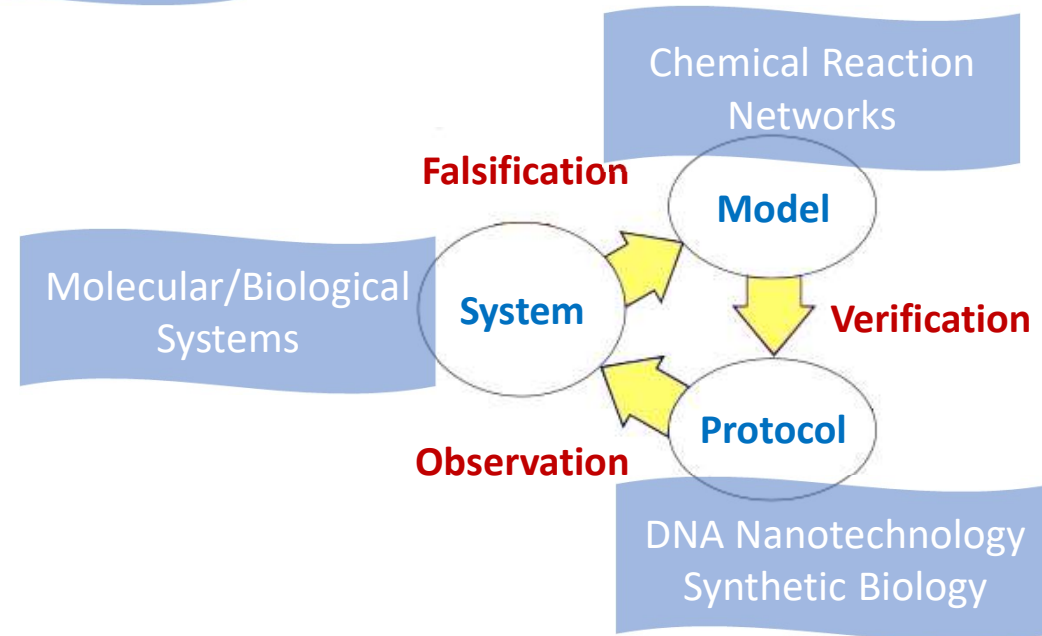
- Performance evaluation/optimization: of model+protocol+system combined
- Management: version control, equipment monitoring, data storage



The Inner Loop

- A specific domain
- Aiming for **closed-loop automated modelling and experimentation**
- Via Molecular Programming

In this talk

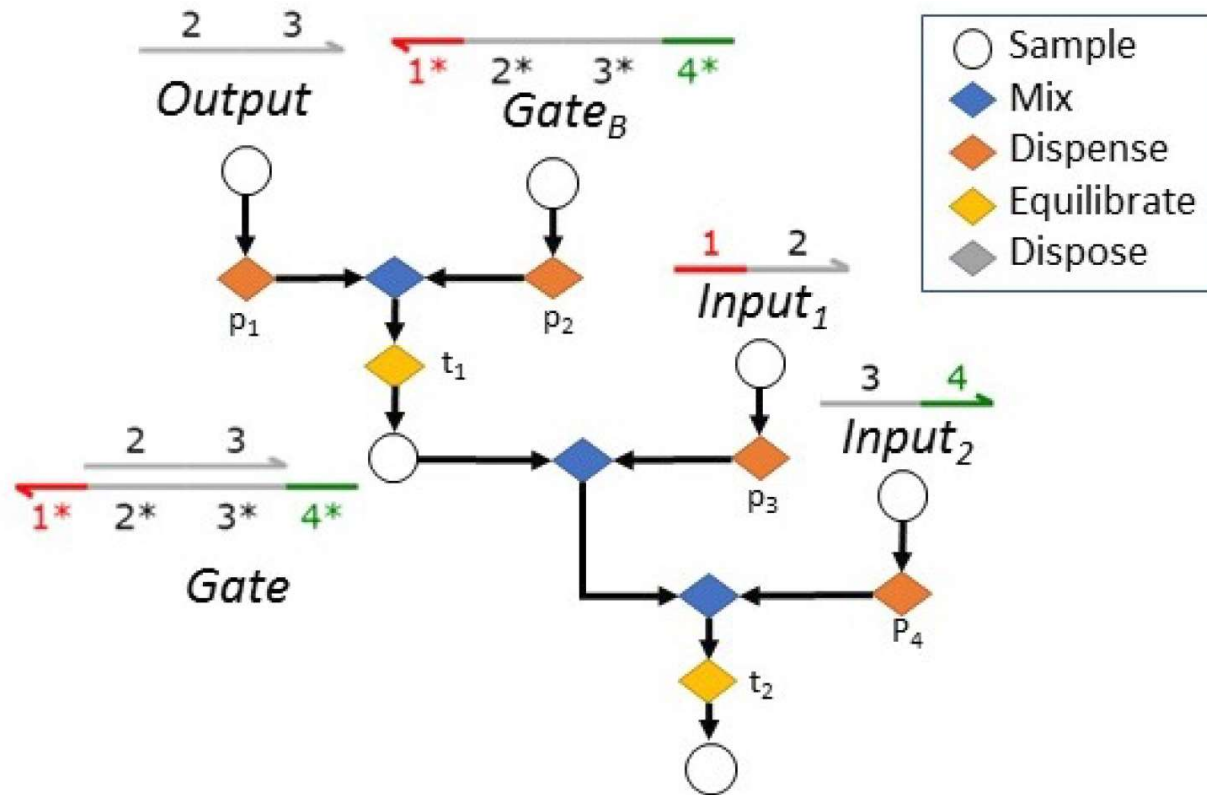


Protocols

(lab procedures that know nothing about models)

A Protocol

For DNA gate assembly and activation in vitro



← Protocol steps
(liquid handing)

Digital Microfluidics

Manipulating droplets by electrical fields

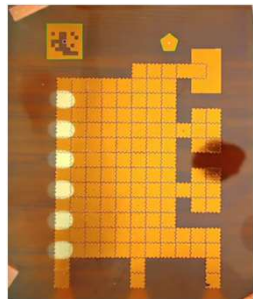
OpenDrop

<https://www.youtube.com/watch?v=ncfZWqPm7-4>



OpenDrop speed test

https://www.youtube.com/watch?v=pSIs9L_h3Q0



Purple Drop (UW)

<https://misl.cs.washington.edu/projects/fluidics.html>

```
a = input(substance_A)
b = input(substance_B)
ab = mix(a, b)
```

```
while get_pH(ab) > 7:
    heat(ab)
    acidify(ab)
```

Sample program in Python using Puddle.

Digital Microfluidics

- A general, *programmable*, platform to execute the main liquid-handling operations
- To close the cycle, it can support many automated observation techniques on-board or off-board via peripheral pumps (sequencing, mass spec, ...) although these are all very hardware-dependent.

A Protocol Language

Samples: containers with volume, temperature, concentrations

$P =$

x	<i>(a sample variable)</i>
(x_0, V, T)	<i>(initial condition)</i>
$let\ x = P_1\ in\ P_2$	<i>(define local variable)</i>
$Mix(P_1, P_2)$	<i>(mix samples)</i>
$let\ x, y = Split(P_1, p)\ in\ P_2$	<i>(split samples)</i>
$Equilibrate(P, t)$	<i>(equilibrate sample for t seconds)</i>
$Dispose(P)$	<i>(discard sample)</i>

Experimental Biological Protocols with Formal Semantics

Alessandro Abate², Luca Cardelli^{1,2}, Marta Kwiatkowska², Luca Laurenti², and Boyan Yordanov¹

¹ Microsoft Research, Cambridge

² Department of Computer Science, University of Oxford

Protocol Semantics (deterministic)

Each program denotes a *final* state $\langle \text{concentrations, volume, temperature} \rangle$

$\llbracket P \rrbracket^\rho$ is the final state produced by a protocol P where ρ binds its free variables:

$$\llbracket x \rrbracket^\rho = \rho(x)$$

$$\llbracket x_0, V, T \rrbracket^\rho = (x_0, V, T)$$

$$\llbracket Mix(P_1, P_2) \rrbracket^\rho =$$

$$\text{let } (x_0^1, V_1, T_1) = \llbracket P_1 \rrbracket^\rho$$

$$\text{let } (x_0^2, V_2, T_2) = \llbracket P_2 \rrbracket^\rho$$

$$\left(\frac{x_0^1 V_1 + x_0^2 V_2}{V_1 + V_2}, V_1 + V_2, \frac{T_1 V_1 + T_2 V_2}{V_1 + V_2} \right)$$

$$\llbracket \text{let } x = P_1 \text{ in } P_2 \rrbracket^\rho =$$

$$\text{let } (x_0, V, T) = \llbracket P_1 \rrbracket^\rho$$

$$\text{let } \rho_1 = \rho \{x \leftarrow (x_0, V, T)\}$$

$$\llbracket P_2 \rrbracket^{\rho_1}$$

$$\llbracket \text{let } x, y = Split(P_1, p) \text{ in } P_2 \rrbracket^\rho =$$

$$\text{let } (x_0, V, T) = \llbracket P_1 \rrbracket^\rho$$

$$\text{let } \rho_1 = \rho \{x \leftarrow (x_0, V \cdot p, T), y \leftarrow (x_0, V \cdot (1 - p), T)\}$$

$$\llbracket P_2 \rrbracket^{\rho_1}$$

(Equilibrate semantics)

$$\llbracket Dispose(P) \rrbracket^\rho = (0^{|A|}, 0, 0),$$

(CRN semantics)

Summarizing

- Our protocols are (liquid handling) programs
- We can compute their behavior (their final state)
- We can (virtually) run them (by simulation)
- We can (physically) run them (e.g., by digital microfluidics)

Models

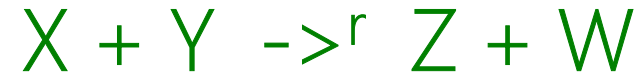
(equations that know nothing about protocols)

We could choose Differential Equations as our modeling language, as in most of science.

Instead, we choose Chemical Reaction Networks (this is roughly equivalent).

Anyway, in order to "*implement differential equations*" we need to "*implement chemical reactions*" (or some other physical realization).

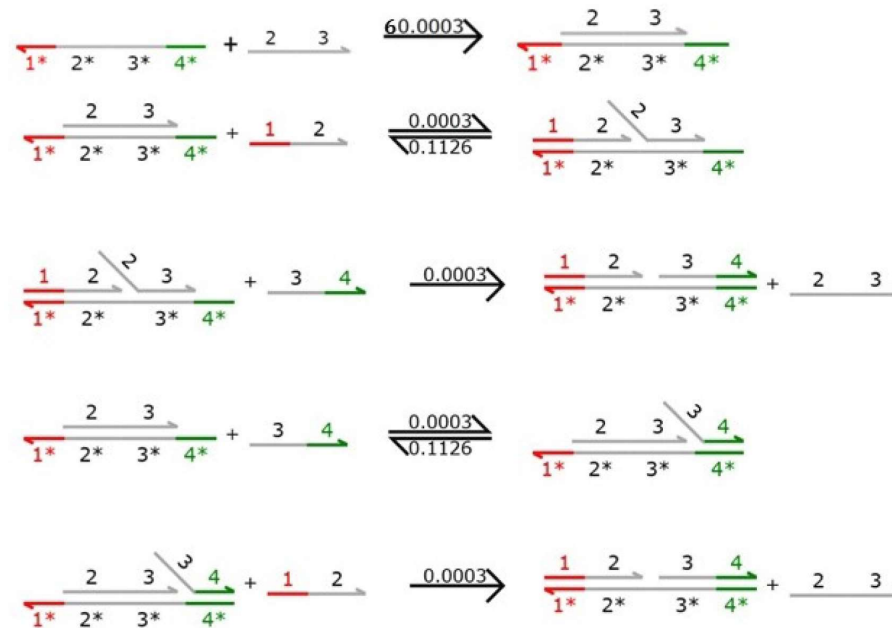
Chemical Reaction Networks (CRN)



- A *phenomenological model* of kinetics in the natural sciences
By (only) observing naturally occurring reactions
- A *programming language*, finitely encoded in the genome
By which living things manage the *unbounded* processing of matter and information
- A *mathematical structure*, rediscovered in many forms
Vector Addition Systems, Petri Nets, Bounded Context-Free Languages, Population Protocols, ...
- A description of *mechanism* (“instructions” / “interactions”) rather than *behavior* (“equations” / “approximations”)
Although the two are related in precise ways
Enabling, e.g., the study of the evolution of *mechanism* through unchanging *behavior*

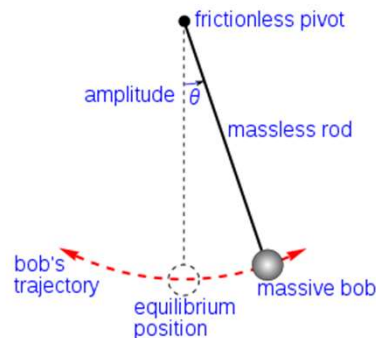
E.g., a CRN model of DNA interactions

- Strand displacement reaction between DNA strands



- (It says nothing about the protocols we just saw)

Programming ^{"elementary"} *any* dynamical system as a CRN



Galileo Galilei 1602
Christiaan Huygens 1673

$$\partial^2\theta = -g/l \sin\theta$$

Equation of motion of
the simple pendulum

<https://en.wikipedia.org/wiki/Pendulum>

A *dynamical systems* is anything characterized by a system of differential equations (ODEs).

Elementary dynamical systems are those that include on the r.h.s. only polynomials, trigonometry, exponentials, fractions, and their inverses.

(All of biochemistry, all of electronics, most of physics, deterministic chaos, etc.)

STEP 1, Polynomization: Elementary ODEs can be exactly reduced to just polynomial ODEs.

MATHEMATICAL THEORY OF THE DIFFERENTIAL
ANALYZER

BY CLAUDE E. SHANNON

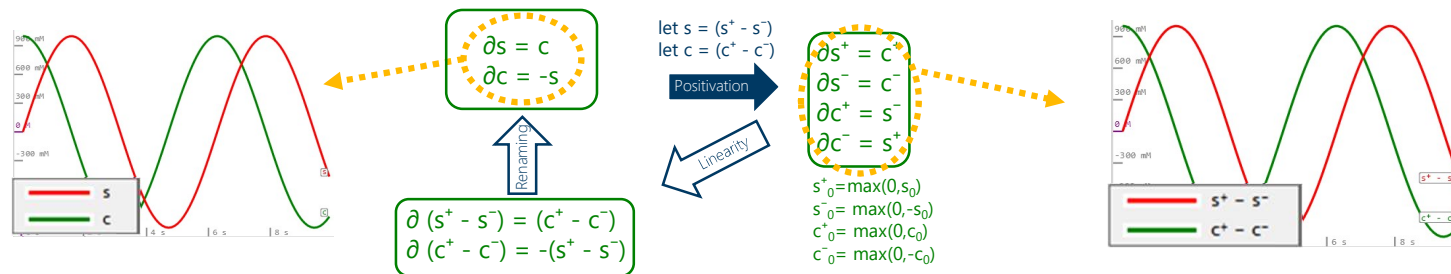
Abstraction of Elementary Hybrid Systems by Variable
Transformation

Jiang Liu¹, Najun Zhan², Hengjun Zhao¹, and Liang Zou²

"elementary"

Programming *any* dynamical system as a CRN

Consider *the* canonical polynomial oscillator: sine/cosine



A very simple elementary ODE system.

But variables go negative: we can't have that in a CRN (no negative concentrations).

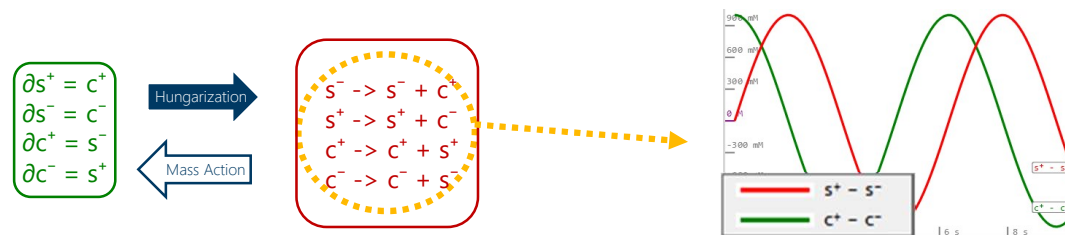
STEP 2, Positivation: Split potentially negative variables of polynomial ODEs into the difference of two positive variables. Obtain the same trajectories as differences.

Biomolecular implementation of linear I/O systems

K. Oishi E. Klavins

Programming ^{"elementary"} *any* dynamical system as a CRN

Translate positive ODEs to chemical reactions



The Law of Mass Action tells us how to produce polynomial ODEs from CRNs. The inverse process is called Hungarization, it works for *Hungarian* ODEs (polynomial ODEs where each negative monomial has the l.h.s. differentiated variable as a factor).

STEP 3, Hungarization: Translate polynomial ODEs to chemical reaction networks: each monomial on the r.h.s. produces one reaction.

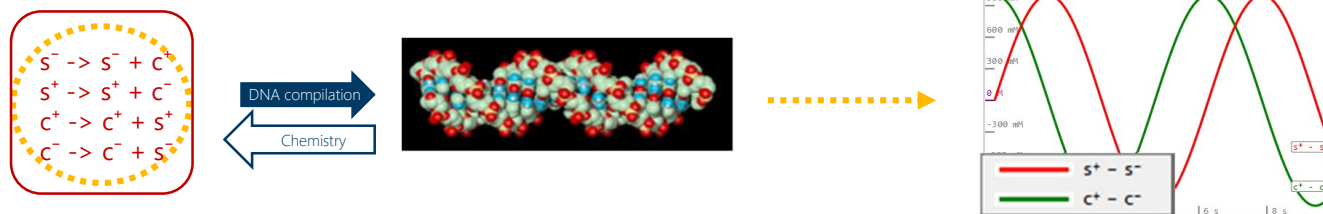
ON THE INVERSE PROBLEM OF REACTION KINETICS
V. HÁRS - J. TÓTH

Subject to the ODEs being *Hungarian*, but that is always satisfied after positivation!

E.g. the Lorenz chaotic attractor is already polynomial but not Hungarian, it cannot be translated to mass action reactions without first doing positivation.

Programming *any*^{"elementary"} dynamical system as a CRN

Translate those CRNs to (real, DNA) molecules



Chemistry tells us (sometimes) what reactions molecules obey.

The inverse process is possible for DNA molecules, because we can "program" them.

STEP 4, Molecular programming: Translate any mass action chemical reaction network into a set of DNA molecules that obey those reactions.

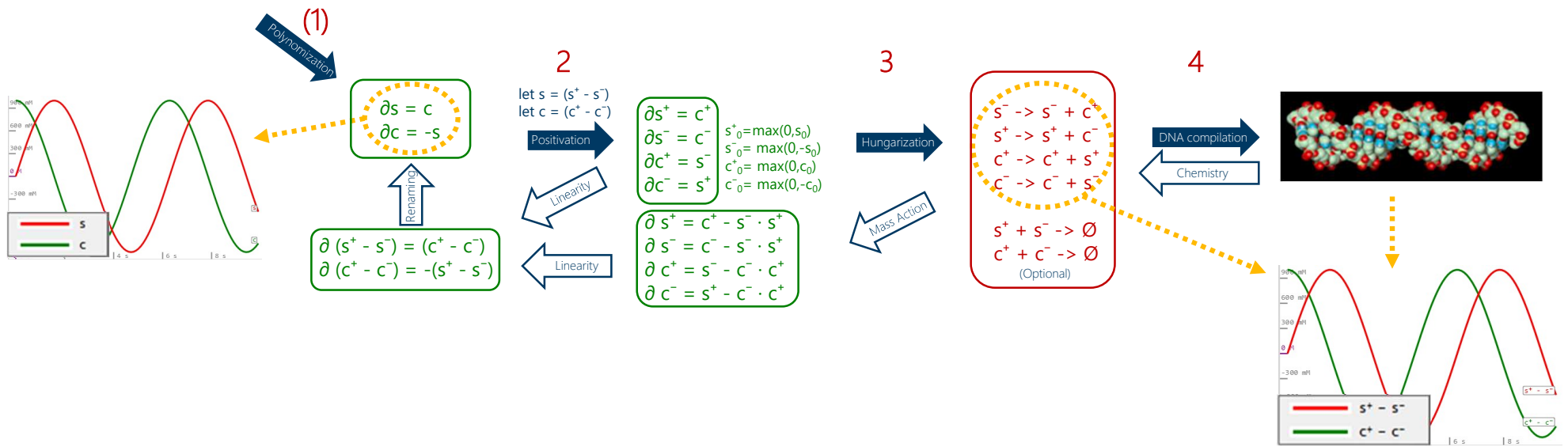
Works up to an arbitrarily good approximation of Mass Action kinetics, and up to time rescaling.

DNA as a universal substrate for chemical kinetics

David Soloveichik, Georg Seelig, and Erik Winfree
PNAS March 23, 2010 107 (12) 5393-5398; <https://doi.org/10.1073/pnas.0909380107>

Programming *any* ^{"elementary"} dynamical system as a CRN

Thus, CNRs are "Shannon complete", and can be physically realized



Programming ^{"elementary"} *any* dynamical system as a CRN

- Chemistry is (also) a formal language that we can use to implement ~*any* dynamical system with *real* (DNA) molecules
- Approaching a situation where we can "systematically compile" (synthesize) a model to DNA molecules, run an (automated) protocol, and observe (sequence) the results in a closed loop.
- N.B.: DNA can be used to manipulate and organize programmatically **other forms of matter**, so this is not really restricted to DNA experiments.

Model Semantics (deterministic)

- ODE semantics of CRNs

Definition (CRN Flux) Let $(\mathcal{A}, \mathcal{R})$ be a CRN. Let $F(V, T) \in \mathbb{R}_{\geq 0}^{|\mathcal{A}|} \rightarrow \mathbb{R}^{|\mathcal{A}|}$ be the flux of the CRN at volume $V \in \mathbb{R}_{> 0}$ and temperature $T \in \mathbb{R}_{\geq 0}$. For a concentration vector $\mu \in \mathbb{R}_{\geq 0}^{|\mathcal{A}|}$ we assume $F(V, T)(\mu) = \sum_{\tau \in \mathcal{R}} v_{\tau} \alpha_{\tau}(V, T, \mu)$; with stoichiometric vector v_{τ} and rate function α_{τ} .

Law of Mass Action $F(V, T)$ makes up the r.h.s. of an ODE system $\partial \mathcal{A} = F(V, T)$

State produced by a CRN $\mathcal{C} = (\mathcal{A}, \mathcal{R})$ (species \mathcal{A} , reactions \mathcal{R})

with flux F (r.h.s. of its mass action ODEs) at time t ,

from initial state (x_0, V, T) (initial concentrations x_0 , volume V , temperature T):

$$\llbracket ((\mathcal{A}, \mathcal{R}, x_0), V, T) \rrbracket (H)(t) = (G(t), V, T)$$

$$\text{let } G : [0 \dots H) \rightarrow \mathbb{R}^{|\mathcal{A}|} \text{ be the solution of } G(t') = x_0 + \int_0^{t'} F(V, T)(G(s)) ds$$

Summarizing

- Our models are (chemical) programs
 - We can compute their behavior (their final state)
 - We can (virtually) run them by integration of the ODEs
 - We can (physically) run them by DNA nanotech
-
- Recall: we are aiming for models that can be placed into a closed-loop automated model+protocol cycle.

Models *together with* Protocols

An Integrated Description

Samples: containers with volume, temperature, concentrations

$P =$

x (a sample variable)

(x_0, V, T) (initial condition)

let $x = P_1$ in P_2 (define local variable)

$Mix(P_1, P_2)$ (mix samples)

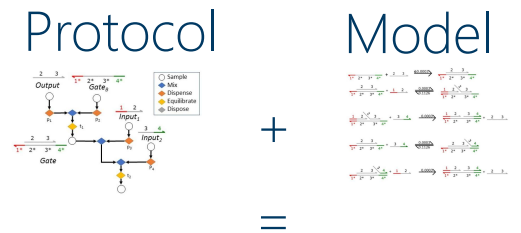
let $x, y = Split(P_1, p)$ in P_2 (split samples)

$Equilibrate(P, t)$ (equilibrate sample for t seconds)

$Dispose(P)$ (discard sample)

each sample evolves (via *Equilibrate*) according to a given overall CRN:

$\mathcal{C} = (\mathcal{A}, \mathcal{R})$ (species, reactions)



Joint script

```

Input1 = < 1* 2 >   Output = < 2 3 >
Input2 = < 3 4* >   Gate = {1*}[2 3]{4*}

P1 = let In1 = ((Input1, 100.0nM), 0.1mL, 25.0°C) in
let In2 = ((Input2, 100.0nM), 0.1mL, 25.0°C) in
let GA = ((Output, 100.0nM), 0.1mL, 25.0°C) in
let GB = ((Gate, 100.0nM), 0.1mL, 25.0°C) in
let sGA, = Dispense(GA, p1) in
let sGB, = Dispense(GB, p2) in
let sIn1, = Dispense(In1, p3) in
let sIn2, = Dispense(In2, p4) in
Observe(Equilibrate(Mix(Mix(Equilibrate(
Mix(sGA, sGB), t1), sIn1), sIn2), t2), idn).
    
```

Program Semantics (deterministic)

Each program denotes a *final* state $\langle \text{concentrations, volume, temperature} \rangle$

Experimental Biological Protocols with Formal Semantics

Alessandro Abate², Luca Cardelli^{1,2}, Marta Kwiatkowska², Luca Laurenti², and Boyan Yordanov¹

¹ Microsoft Research, Cambridge
² Department of Computer Science, University of Oxford

$\llbracket P \rrbracket^\rho$ is the final state produced by a protocol P for a fixed CRN $\mathcal{C} = (\mathcal{A}, \mathcal{R})$:

$$\llbracket x \rrbracket^\rho = \rho(x)$$

$$\llbracket x_0, V, T \rrbracket^\rho = (x_0, V, T)$$

$$\llbracket \text{Mix}(P_1, P_2) \rrbracket^\rho =$$

$$\text{let } (x_0^1, V_1, T_1) = \llbracket P_1 \rrbracket^\rho$$

$$\text{let } (x_0^2, V_2, T_2) = \llbracket P_2 \rrbracket^\rho$$

$$\left(\frac{x_0^1 V_1 + x_0^2 V_2}{V_1 + V_2}, V_1 + V_2, \frac{T_1 V_1 + T_2 V_2}{V_1 + V_2} \right)$$

$$\llbracket \text{let } x = P_1 \text{ in } P_2 \rrbracket^\rho =$$

$$\text{let } (x_0, V, T) = \llbracket P_1 \rrbracket^\rho$$

$$\text{let } \rho_1 = \rho \{ x \leftarrow (x_0, V, T) \}$$

$$\llbracket P_2 \rrbracket^{\rho_1}$$

$$\llbracket \text{let } x, y = \text{Split}(P_1, p) \text{ in } P_2 \rrbracket^\rho =$$

$$\text{let } (x_0, V, T) = \llbracket P_1 \rrbracket^\rho$$

$$\text{let } \rho_1 = \rho \{ x \leftarrow (x_0, V \cdot p, T), y \leftarrow (x_0, V \cdot (1 - p), T) \}$$

$$\llbracket P_2 \rrbracket^{\rho_1}$$

$$\llbracket \text{Equilibrate}(P, t) \rrbracket^\rho =$$

$$\text{let } (x_0, V, T) = \llbracket P \rrbracket^\rho$$

$$\llbracket (\mathcal{A}, \mathcal{R}, x_0), V, T \rrbracket(H)(t)$$

$$\llbracket \text{Dispose}(P) \rrbracket^\rho = (0^{|\mathcal{A}|}, 0, 0),$$

State produced by CRN $\mathcal{C} = (\mathcal{A}, \mathcal{R})$ with flux F at time t :

$$\llbracket (\mathcal{A}, \mathcal{R}, x_0), V, T \rrbracket(H)(t) =$$

$$\text{let } G : [0 \dots H] \rightarrow \mathbb{R}^{|\mathcal{A}|} \text{ be the solution of } G(t') = x_0 + \int_0^{t'} F(V, T)(G(s)) ds$$

$$(G(t), V, T)$$

A Joint Semantics

This semantics gives us a *joint simulation algorithm*, connecting chemical simulation with protocol simulation.

In this presentation everything is *deterministic*. The state of the protocol is passed to the chemical simulator, which computes a new state that it passes to the protocol simulator, and so on.

We can also define a joint *stochastic* simulation, passing mean and variance information back and forth between chemical and protocol simulation.

This requires an extension of the above semantics using the *Linear Noise Approximation* of chemical kinetics, which computes mean and variance of concentrations (both by ODEs, not e.g. by Gillespie algorithm), and a similar extension of the protocol operations.

Program Semantics (stochastic)

Each program denotes a *final* state $\langle \text{concentrations}, \text{covariances}, \text{volume}, \text{temperature} \rangle$

A Language for Modeling and Optimizing Experimental Biological Protocols

Luca Cardelli ^{*}, Marta Kwiatkowska and Luca Laurenti [†]

Definition 3. (CRN Flux) Let $(\mathcal{A}, \mathcal{R})$ be a CRN. Let $F(V, T) \in \mathbb{R}_{\geq 0}^{|\mathcal{A}|} \rightarrow \mathbb{R}^{|\mathcal{A}|}$ be the flux of the CRN at volume $V \in \mathbb{R}_{\geq 0}$ and temperature $T \in \mathbb{R}_{\geq 0}$. For a concentration vector $\mu \in \mathbb{R}_{\geq 0}^{|\mathcal{A}|}$ we assume $F(V, T)(\mu) = \sum_{\tau \in \mathcal{R}} v_{\tau} \alpha_{\tau}(V, T, \mu)$, with stoichiometric vector v_{τ} and rate function α_{τ} . We call J_F the Jacobian of $F(V, T)$, and J_F^{\top} its transpose. Further, define $W(V, T)(\mu) = \sum_{\tau \in \mathcal{R}} v_{\tau} v_{\tau}^{\top} \alpha_{\tau}(V, T, \mu)$ to be the diffusion term.

Definition 4. (CRN Time Evolution) Given a CRS $(\mathcal{A}, \mathcal{R})$, (μ, Σ, V, T) , its evolution at time $t < H$ (where $H \in \mathbb{R}_{\geq 0} \cup \{\infty\}$ is a time horizon) is the state $(\mu_{\mu}(t), \Sigma_{\mu, \Sigma}(t), V, T)$ obtained by integrating its flux up to time t , where:

$$\mu_{\mu}(t) = \mu + \int_0^t F(V, T)(\mu_{\mu}(s)) ds \quad (1)$$

$$\Sigma_{\mu, \Sigma}(t) = \Sigma + \int_0^t J_F(\mu_{\mu}(s)) \Sigma_{\mu, \Sigma}(s) + \Sigma_{\mu, \Sigma}(s) J_F^{\top}(\mu_{\mu}(s)) + W(V, T)(\mu_{\mu}(s)) ds, \quad (2)$$

with $\mu_{\mu}(0) = \mu$ and $\Sigma_{\mu, \Sigma}(0) = \Sigma$. If, for such an H , μ or Σ are not unique, then we say that the evolution is ill-posed. Otherwise, $\mu_{\mu}(t)$ and $\Sigma_{\mu, \Sigma}(t)$ define a Gaussian process with that mean and covariance matrix for $t < H$.



$$\llbracket x \rrbracket^{\rho} = \rho(x)$$

$$\llbracket (p_1 \dots p_{|\mathcal{A}|}, r_V, r_T) \rrbracket^{\rho} = (\llbracket p_1 \rrbracket^{\rho} \dots \llbracket p_{|\mathcal{A}|} \rrbracket^{\rho}, 0^{|\mathcal{A}| \times |\mathcal{A}|}, r_V, r_T)$$

$$\llbracket \text{let } x = P_1 \text{ in } P_2 \rrbracket^{\rho} = \llbracket P_2 \rrbracket^{\rho_1}$$

$$\text{where } \rho_1 = \rho \{ x \leftarrow \llbracket P_1 \rrbracket^{\rho} \}$$

$$\llbracket \text{Mix}(P_1, P_2) \rrbracket^{\rho} = \left(\frac{V_1 \mu_1 + V_2 \mu_2}{V_1 + V_2}, \frac{V_1^2 \Sigma_1 + V_2^2 \Sigma_2}{(V_1 + V_2)^2}, V_1 + V_2, \frac{V_1 T_1 + V_2 T_2}{V_1 + V_2} \right)$$

$$\text{where } (\mu_1, \Sigma_1, V_1, T_1) = \llbracket P_1 \rrbracket^{\rho} \text{ and } (\mu_2, \Sigma_2, V_2, T_2) = \llbracket P_2 \rrbracket^{\rho}$$

$$\llbracket \text{let } x, y = \text{Split}(P_1, p) \text{ in } P_2 \rrbracket^{\rho} = \llbracket P_2 \rrbracket^{\rho_1}$$

$$\text{where } r = \llbracket p \rrbracket^{\rho}, \quad 0 < r < 1 \text{ and } (\mu, \Sigma, V, T) = \llbracket P_1 \rrbracket^{\rho}$$

$$\text{and } \rho_1 = \rho \{ x \leftarrow (\mu, \Sigma, rV, T), y \leftarrow (\mu, \Sigma, (1-r)V, T) \}$$

$$\llbracket \text{Equilibrate}(P, p) \rrbracket^{\rho} = (\mu_{\mu}(t), \Sigma_{\mu, \Sigma}(t), V, T)$$

$$\text{where } t = \llbracket p \rrbracket^{\rho} \text{ and } (\mu, \Sigma, V, T) = \llbracket P \rrbracket^{\rho}$$

$$\llbracket \text{Dispose}(P) \rrbracket^{\rho} = (0^{|\mathcal{A}|}, 0^{|\mathcal{A}| \times |\mathcal{A}|}, 0, 0)$$

together with $\llbracket p \rrbracket^{\rho}$ defined as:

$$\llbracket z \rrbracket^{\rho} = \rho(z)$$

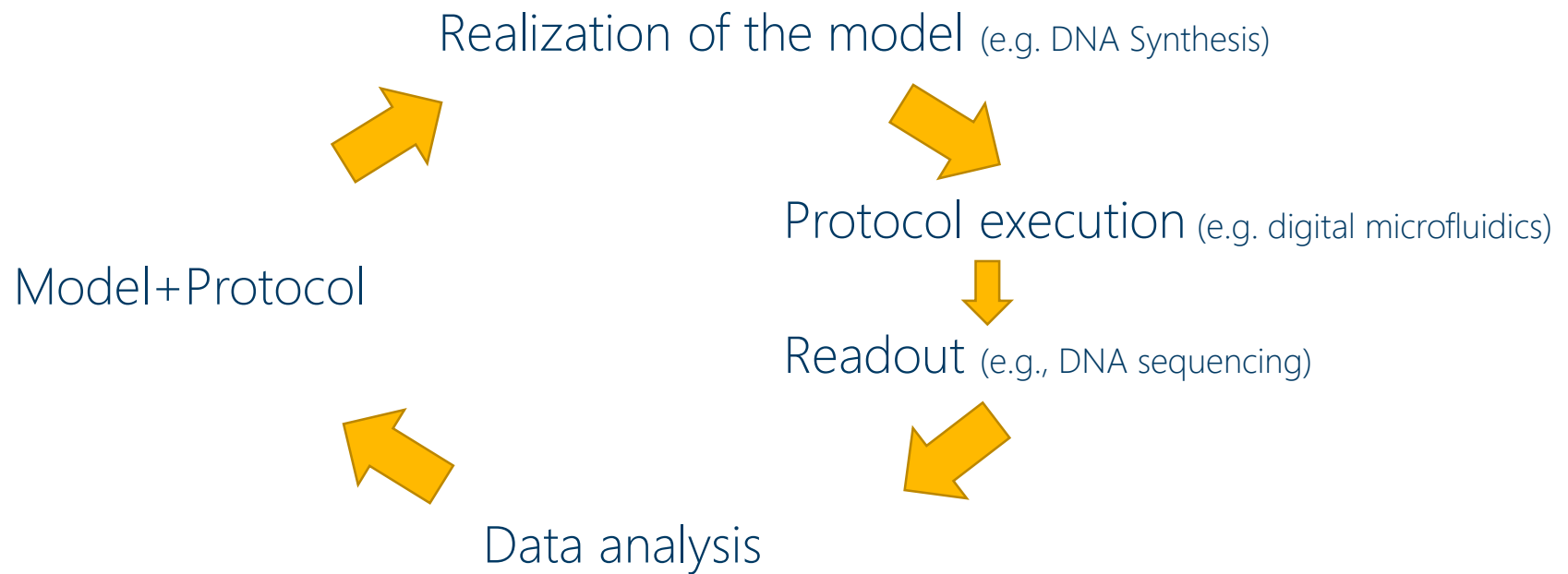
$$\llbracket r \rrbracket^{\rho} = r$$

Stochastic Analysis

- We can ask: what is the probability of a certain outcome given uncertainties in *both the protocol and the model*?
- Conversely: which parameters of *both the protocol and the model* best fit the observed result?
- E.g., we can use Statistical Modelchecking to estimate the probability that the output will fall in a certain range, given the distributions over uncertain model and protocol parameters.

Summarizing

Automated discovery loop:



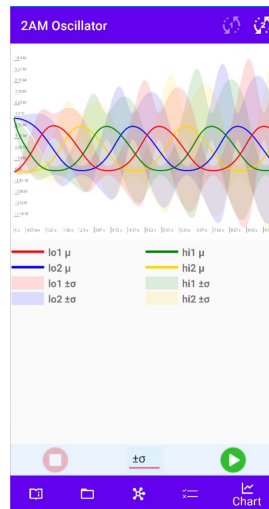
Simulating Reaction Networks together with Digital Protocols

CMSB'2020 Best Tool Paper Award

Kaemika* app
Integrating protocols and chemical simulation

Kaemika

/'kimika/



Search "Kaemika" in the app stores
<http://lucacardelli.name/kaemika.html>



computation



Article

A Language for Modeling and Optimizing Experimental Biological Protocols

Luca Cardelli ^{*}, Marta Kwiatkowska and Luca Laurenti [†]

An integrated language for
chemical models & experimental protocols

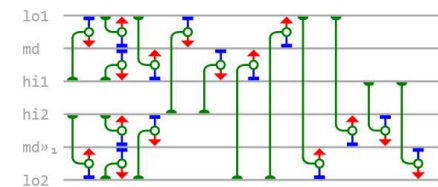
Deterministic (ODE) and
stochastic (LNA) simulation

Chemical reaction networks (CRNs)
and liquid-handling protocols

Reaction scores

Functional scripting

GUI



Main features

- *Species and reactions*
 - Characterized by initial values and rates
- *"Samples" (compartments) and Protocols*
 - Isolate species and reactions in a compartment, and mix compartments
- *Kinetics (simulation)*
 - Deterministic (ODE) or stochastic (LNA) for chemical models
 - Digital microfluidics for chemical protocols
- *Programming abstractions*
 - Assemble models and protocols as compositions of modules

Species and Reactions

```
//=====
// Lotka 1920, Volterra 1926
// (simplified with all rates = 1)
//=====

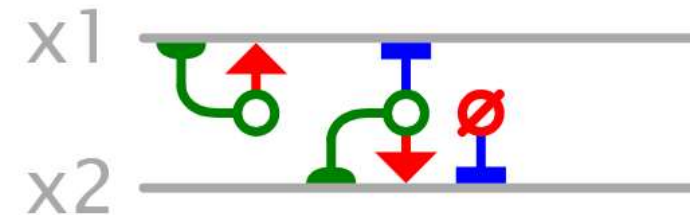
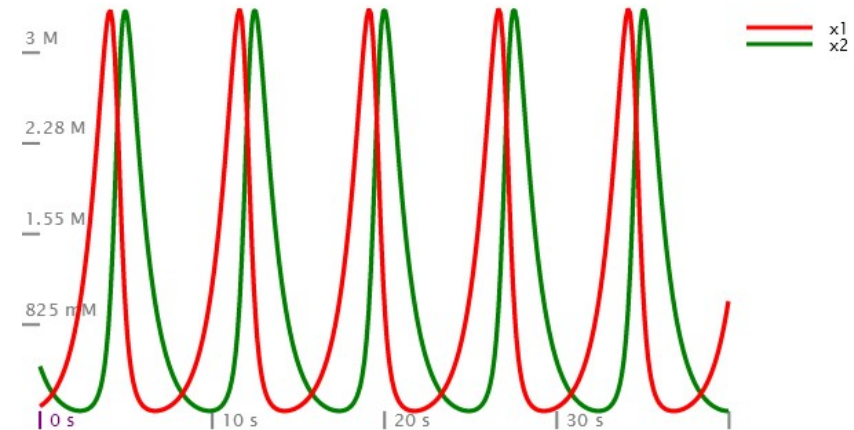
number x1_0 <- uniform(0,1) // random x1_0
number x2_0 <- uniform(0,1) // random x2_0

species x1 @ x1_0 M // prey
species x2 @ x2_0 M // predator

x1 -> x1 + x1 {1} // prey reproduces
x1 + x2 -> x2 + x2 {1} // predator eats prey
x2 -> ∅ {1} // predator dies

equilibrate for 40
```

UNDAMPED OSCILLATIONS, ETC. 1595
UNDAMPED OSCILLATIONS DERIVED FROM THE LAW OF MASS ACTION.
By ALFRED J. LOTKA.
Received June 2, 1920.



Ex: Predatorial (recursive model)

```
function Predatorial(number n) {  
  if n = 0 then  
    define species prey @ 1 M  
    prey -> 2 prey // prey reproduces  
    report prey  
    yield prey  
  else  
    define species predator @ 1/n M  
    species prey = Predatorial(n-1)  
    prey + predator -> {n} 2 predator // predator eats  
    predator -> ∅ // predator dies  
    report predator  
    yield predator  
  end  
}  
  
species apexPredator = Predatorial(5)  
equilibrate for 50
```

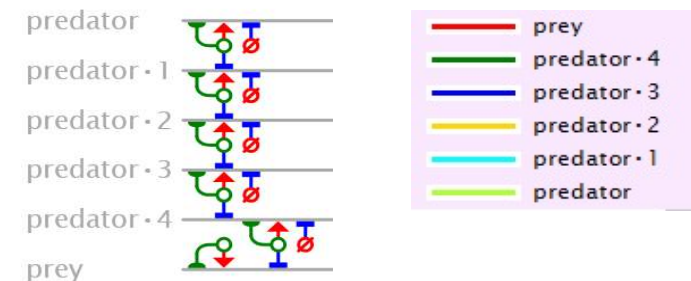
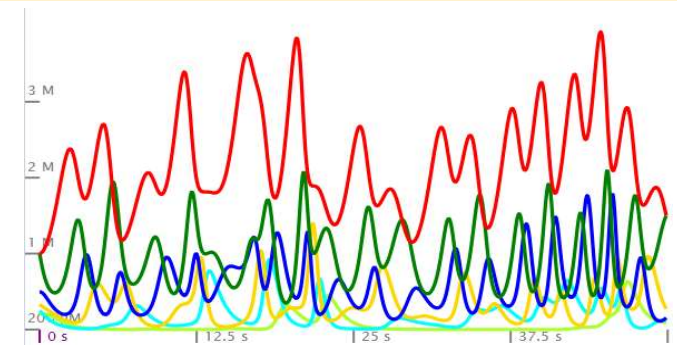
```
//=====
```

```
// Creates a stack of predator-prey
```

```
// relationships in Lotka-Volterra style,
```

```
// and returns the apex predator.
```

```
//=====
```



Extracting the Model and the Protocol

From the script

```
species {c}

sample A
species a @ 1M in A
amount c @ 0.1M in A
a + c -> a + a
equilibrate A1 = A for 1

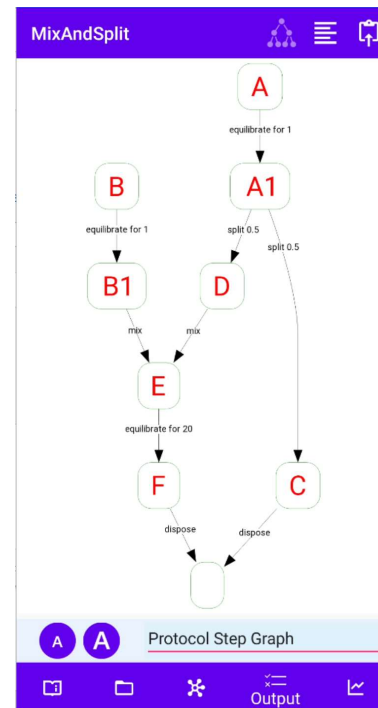
sample B
species b @ 1M in B
amount c @ 0.1M in B
b + c -> c + c
equilibrate B1 = B for 1

split C,D = A1 by 0.5
dispose C

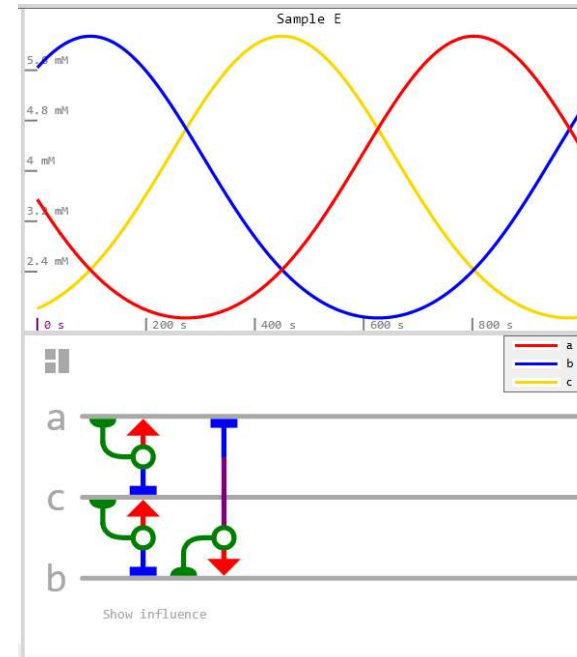
mix E = D with B1
a + b -> b + b

equilibrate F = E for 20
dispose F
```

The protocol



The (final) model (sample E)



```
STATE_5
sample E {1.5mL, 293.2K} {
  a = 354.5mM
  c = 178mM
  b = 0.5674M
  consumed
  a + c -> a + a
  b + c -> c + c
  a + b -> b + b
}

KINETICS for STATE_5 (sample E) for 20 time units:
∂a = a * c - a * b
∂c = c * b - a * c
∂b = a * b - c * b
```


Writing Models Compositionally

- Embedded chemical notation

Programs freely contain both chemical reactions and control flow
Can generate unbounded-size reaction networks

- Rich data types

numbers, species, functions, networks, lists, flows (time-courses)

flows are composable functions of time used in *rates, plotting, and observation*

- Modern abstractions

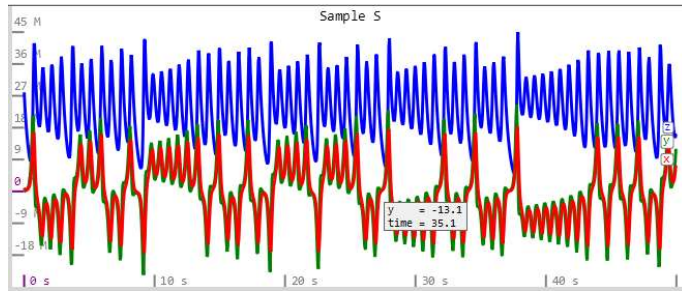
Functional: programs take *data* as parameters and produce *data* as results

Monadic: programs also produce *effects* (*species, reactions, liquid handling*)

Nominal: *lexically scoped* chemical species (species are not "strings")

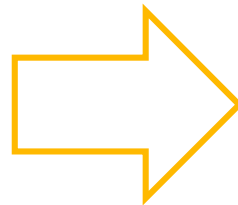
Mass Action Compiler

- Lorenz chaotic attractor

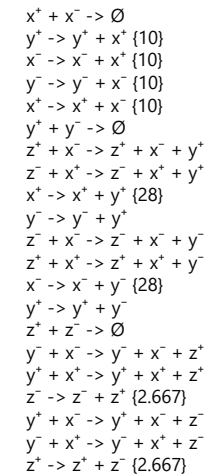
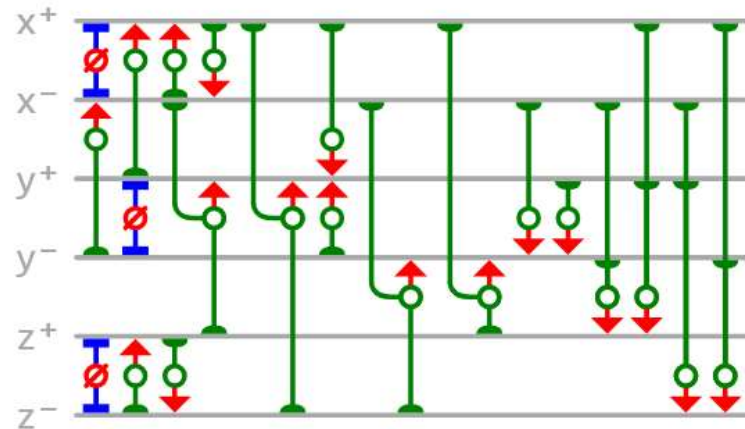


not mass action

$$\begin{aligned} \partial x &= s \cdot y - s \cdot x \\ \partial y &= r \cdot x - x \cdot z - y \\ \partial z &= x \cdot y - b \cdot z \end{aligned}$$



$s = 10$
 $b = 8/3$
 $r = 28$
 $x_0 = 1$
 $y_0 = 0$
 $z_0 = 28$



Initial:
 $x^+ = 1$
 $x^- = 0$
 $y^+ = 0$
 $y^- = 0$
 $z^+ = 28$
 $z^- = 0$

<= Demo: LorenzAttractor

Kaemika Microfluidics Compiler

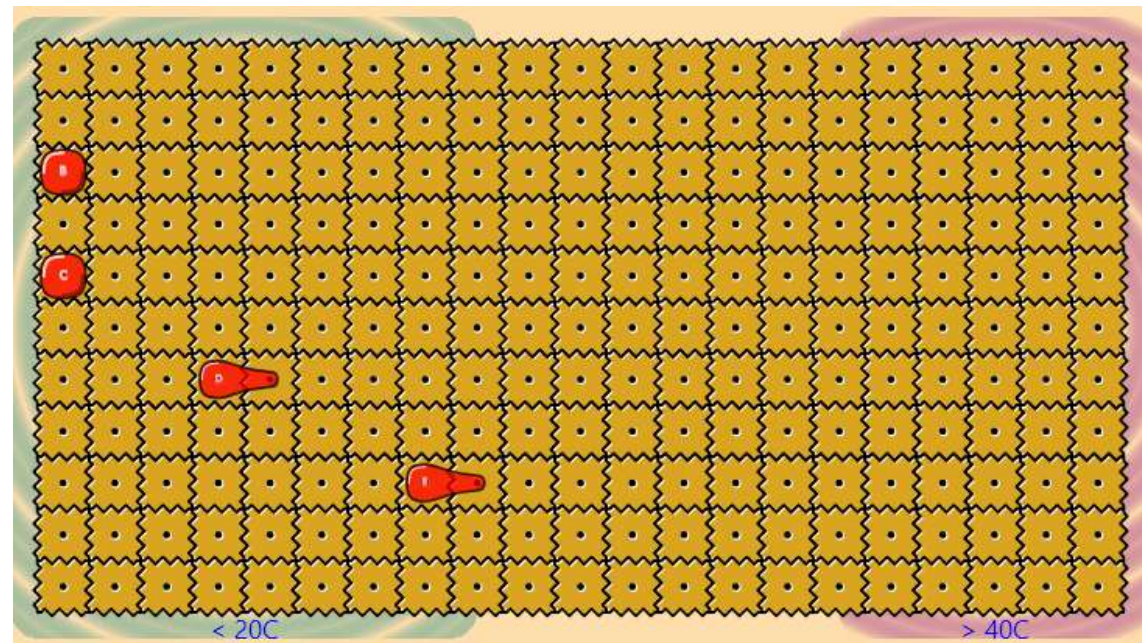
- Mix, split, equilibrate, dispose
- Automatic routing – no geometrical information
- Hot/cold zones

sample A {3 μ L, 20C}

split B,C,D,E = A

mix F = E,C,B,D

dispose F



Conclusions

Integrated modeling

Of chemical reaction networks and protocols

How the Kaemika app supports it

Why it needs a *new language* for smooth integration

Closed-loop modeling, experimentation and analysis

For complete lab automation

To “scale up” the scientific method

A Language for Modeling and Optimizing Experimental Biological Protocols

Luca Cardelli, Marta Kwiatkowska, Luca Laurenti. MDPI Computation 2021.

Experimental biological protocols with formal semantics

Alessandro Abate, Luca Cardelli, Marta Kwiatkowska,
Luca Laurenti, Boyan Yordanov. CMSB 2018.

Kaemika app - Integrating protocols and chemical simulation

Luca Cardelli. CMSB 2020.

Kaemika User Manual

<http://lucacardelli.name/Papers/Kaemika%20User%20Manual.pdf>